# Inferring a Relax NG Schema from XML Documents

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**Abstract.** An XML schema specifies the structural properties of XML documents generated from the schema and, thus, is useful to manage XML data efficiently. However, there are often XML documents without a valid schema or with an incorrect schema in practice. This leads us to study the problem of inferring a Relax NG schema from a set of XML documents that are presumably generated from a specific XML schema. Relax NG is an XML schema language developed for the next generation of XML schema Definitions (XSDs). Regular hedge grammars accept regular tree languages and the design of Relax NG is closely related with regular hedge grammars. We develop an XML schema inference system using hedge grammars. We employ a genetic algorithm and state elimination heuristics in the process of retrieving a concise Relax NG schema. We present experimental results using real-world benchmark.

Keywords: XML schema inference  $\cdot$  Regular hedge grammar  $\cdot$  Relax NG  $\cdot$  Genetic algorithm

#### 1 Introduction

Most information in the real-world has structured with linear ordering and hierarchies. Structural information is often represented in XML (Extensible Markup Language) format, which is both human-readable and machine-readable. An XML schema describes properties and constraints about XML documents. We can manipulate XML data efficiently if we know the corresponding XML schema for the input XML data [11,16,20]. Many researchers demonstrated several advantages when the corresponding XML schema exists [14,21].

All valid XML documents should conform to a DTD or a XML schema. However, in practice, we may not have a valid schema or have an incorrect schema or have an incorrect schema for an input XML data [2,17]. For these reasons, there were several attempts to infer a valid XML schema from a given XML data [3–5]. Bex et al. [3,4] presented an idea for learning deterministic regular expressions for inferring *document type definitions* (DTDs) concisely from XML documents. Bex et al. [5] designed an algorithm for inferring *XML Schema Definitions* (XSDs), which are more powerful than DTDs, from XML documents. We consider a schema language called *Relax NG*, which is more powerful than both DTDs and XSDs [19]—due to its expressive power, researchers proposed several applications based on Relax NG schema language [1,15]. League and Eng [15] proposed a compression technique of XML data with a Relax NG schema and showed its effectiveness, especially, for highly tagged and nested data.

We study the problem of inferring a concise Relax NG schema from XML documents based on the genetic algorithm approach. Note that a XML document can be described as an ordered tree. Then a Relax NG schema is a regular tree language. Therefore, we use normalized regular hedge grammars (NRHGs) [18] as theoretical tools for representing Relax NG schema since NRHGs exactly captures the class of regular tree languages. We employ a genetic algorithm for learning NRHGs from a set of trees and design a conversion algorithm for obtaining a concise Relax NG schema from NRHGs.

The main idea of inferring a Relax NG schema consists of the following three steps:

- 1. construct an initial NRHG that only generates all positive instances,
- 2. reduce the size of the NRHG using genetic algorithm while considering all negative examples, and
- 3. convert the obtained NRHG into a concise Relax NG schema with the help of state elimination algorithm and variable dependency computation.

We present experimental results with three benchmark schemas and show the preciseness and conciseness of our approach. Our Relax NG inference system successfully infers three benchmark schemas with instances randomly generated by a Java library called xmlgen. We measure the accuracy of our inference algorithm by validating XML documents generated from the original schema against the inferred schema. The inferred schema accepts about 90 % of positive examples and rejects about 80 % of negative examples.

We give some basic notations and definitions in Sect. 2, and present a technique for inferring an NRHG from a set of positive examples in Sect. 3. In Sect. 4, we present a conversion algorithm that converts an NRHG into a Relax NG schema. Experimental results are presented in Sect. 5.

#### 2 Preliminaries

Let  $\Sigma$  be a finite alphabet and  $\Sigma^*$  be the set of all strings over the alphabet  $\Sigma$  including the empty string  $\lambda$ . The size  $|\Sigma|$  of  $\Sigma$  is the number of characters in  $\Sigma$ . For a string  $w \in \Sigma^*$ , we denote the length of w by |w| and the *i*th character of w by  $w_i$ . A language over  $\Sigma$  is any subset of  $\Sigma^*$ .

Let t be a tree,  $t_n$  be the number of nodes in t and  $t_e$  be the number of edges in t. We define the size |t| of a tree t to be  $t_n + t_e$ , which is the number of nodes and edges in t. The root node of t is denoted by  $t_{\text{root}}$ . Let v be a node of a tree. Then, we denote the parent node of v by  $v_{\text{parent}}$ , the left sibling of v by  $v_{\text{sibling}}$ , and the *i*th child of v by v[i]. We also denote the number of children of the node v by  $|v_{\text{child}}|$  and the label of a node v by |abel(v). A regular expression over  $\Sigma$  is  $\emptyset, \lambda$ , or  $a \in \Sigma$ , or is obtained by applying the following rules finitely many times. For two regular expressions  $R_1$  and  $R_2$ , the union  $R_1 + R_2$ , the catenation  $R_1 \cdot \mathcal{R}_2$ , and the star  $R_1^*$  are regular expressions.

A nondeterministic finite-state automaton (NFA) A is specified by a tuple  $(Q, \Sigma, \delta, s, F)$ , where Q is a finite set of states,  $\Sigma$  is an input alphabet,  $\delta : Q \times \Sigma \to 2^Q$  is a multi-valued transition function,  $s \in Q$  is the initial state and  $F \subseteq Q$  is a set of final states. The transition function  $\delta$  can be extended to a function  $Q \times \Sigma^* \to 2^Q$  that reflects sequences of inputs. A string w over  $\Sigma$  is accepted by A if there is a labeled path from s to a state in F such that this path spells out the string w; namely,  $\delta(s, w) \cap F \neq \emptyset$ . The language L(A) recognized by A is the set of all strings that are spelled out by paths from s to a final state in  $F: L(A) = \{w \in \Sigma^* \mid \delta(s, w) \cap F \neq \emptyset\}.$ 

A normalized regular hedge grammar (NRHG) G is specified by a quintuple  $(\Sigma, V_T, V_F, P, s)$ , where  $\Sigma$  is an alphabet,  $V_T$  is a finite set of tree variables,  $V_F$  is a finite set of forest variables,  $s \in V_T$  is the starting symbol, and P is a set of production rules, each of which takes one of the following four forms:

- (a)  $v_t \to x$ , where  $v_t$  is a tree variable in  $V_T$ , and x is a terminal in  $\Sigma$ ,
- (b)  $v_t \to x \langle v_f \rangle$ , where  $v_t$  is a tree variable in  $V_T$ , x is a terminal in  $\Sigma$  and  $v_f$  is a forest variable in  $V_F$ ,
- (c)  $v_f \rightarrow v_t$ , where  $v_f$  is a forest variable and  $v_t$  is a tree variable,
- (d)  $v_f \rightarrow v_t v'_f$ , where  $v_f$  and  $v'_f$  are forest variables and  $v_t$  is a tree variable.

We consider a *derivation* of NRHGs. Given a sequence of variables, we repeatedly replace variables with productions on the right-hand side.

- 1. for a production rule  $v_t \to x$ , a node labeled by  $x \in \Sigma$  is derived from the tree variable  $v_t$ ,
- 2. for a production rule  $v_t \to x \langle v_f \rangle$ , a tree with a root node labeled by x and its child node  $v_f$  is derived from  $v_t$ ,
- 3. for a production rule  $v_f \rightarrow v_t$ , a node  $v_t$  is derived from  $v_f$ , and
- 4. for a production  $v_f \to v_t v'_f$ , a sequence of nodes  $v_t$  and  $v'_f$  is derived from  $v_f$ .

The language generated by G is the set of trees derived from s. Given an NRHG  $G = (\Sigma, V_T, V_F, P, s)$ , the size |G| of G to be  $|V_T| + |V_F| + |P|$ . Note that the NRHGs generate *regular tree languages* of unranked trees. Thus an NRHG can be converted into an unranked tree automaton and vice versa [6].

For more knowledge in automata and formal language theory, the reader may refer to the textbooks [12,22].

### 3 Inference of an NRHG from Trees

A XML document is useful to store a structured information and, often, represented as a labeled and ordered tree. Given a set of positive examples (trees) and a set of negative examples, we aim at learning an NRHG that generates all positive examples and does not generate all negative examples. Let T be a given set of examples,  $T_+ \subseteq T$  denote the set of positive examples and  $T_- \subseteq T$  be a set of negative examples. First, we construct *primitive NRHGs* from positive examples; For each tree  $t \in T_+$ , we construct an NRHG  $G_t$  that only accepts the tree t. Namely,  $L(G_t) = \{t\}$ . Then, we take the union of all primitive NRHGs and construct an NRHG  $G_{T_+}$  that only accepts all positive examples, that is,

$$L(G_{T_+}) = \bigcup_{t \in T_+} L(G_t).$$

We reduce the size of the resulting NRHG by merging variables using a genetic algorithm. Note that the problem of minimizing the NRHG is at least as hard as any PSPACE-complete problem as the problem of minimizing NFAs is PSPACE-complete [13]. Therefore, we rely on the genetic algorithm approach to reduce the size of very large primitive NRHGs as much as possible.

#### 3.1 Primitive NRHG Construction

We present a linear-time algorithm for constructing a primitive NRHG that only accepts a given tree t. Our algorithm runs recursively from the root node of t to the leaf nodes.

For each node of t, we recursively construct an NRHG according to the number of children of t. If a node v labeled by x has no child, then we create a production rule  $T \to x$ . If a node v labeled by x has more than one child, then we create a production rule  $T \to x\langle F \rangle$ . Then, we make a forest variable Fto generate the sequence of subtrees of v. Let us assume that v has n subtrees from  $t_1$  to  $t_n$  and a tree variable  $T_i$  generates a subtree  $t_i$ . Then, by creating the following variables and production rules, we let F generate the sequence of subtrees:  $F \to T_1F_1$ ,  $F_1 \to T_2F_2$ ,  $\cdots F_{n-2} \to T_{n-1}F_{n-1}$ ,  $F_{n-1} \to T_n$ . Since each node in t is represented by a tree variable, each edge in t is represented by a forest variable and left side of each production rule is a tree variable or a forest variable,  $|V_T| = t_n$ ,  $|V_F| = t_e$  and  $|P| = |t| = t_n + t_e$ . Therefore, it is easy to verify that the algorithm produces an NRHG  $G = (\Sigma, V_T, V_F, P, s)$  in O(|t|)time such that L(G) = t, where  $|V_T| = t_n$ ,  $|V_F| = t_e$ , and |P| = |t|.

Suppose that we have n positive examples from  $t_1$  to  $t_n$ . We first construct n primitive NRHGs called  $G_1$  to  $G_n$ , where  $L(G_i) = \{t_i\}, 1 \le i \le n$ . From the n primitive NRHGs, we take the union of the NRHGs and obtain a single NRHG G such that  $L(G) = \bigcup_{i=1}^n G_i$ . Let  $G_i = (\Sigma_i, V_{T_i}, V_{F_i}, P_i, s_i)$  be an NRHG that accepts  $t_i$ . Then, we construct a new NRHG  $G = (\Sigma, V_T, V_F, P, s)$  that accepts all instances as follows :

$$\Sigma = \bigcup_{i=1}^{n} \Sigma_i, \quad V_T = \bigcup_{i=1}^{n} V_{T_i}, \quad V_F = \bigcup_{i=1}^{n} V_{F_i}, \text{ and } P = \bigcup_{i=1}^{n} P_i.$$

Namely,  $L(G) = \{t_1, t_2, \ldots, t_n\}$ . Then, we merge all occurrences of starting symbols from  $s_1$  to  $s_n$  and denote the merge symbol by s.

#### 3.2 Grammar Optimization by Merging Indistinguishable Variables

Now we have an NRHG  $G = (\Sigma, V_T, V_F, P, s)$  that only generates all positive examples. Since we aim at retrieving a concise Relax NG schema, we need to reduce the size of G as much as possible. As a first step, we find redundant structures from G by identifying *indistinguishable* variables. Given a variable v, which is either in  $V_T$  or  $V_F$ , we define RS(v) to be the set of variables that appear in the right-hand side of production rules, where v appears in the left-hand side. Similarly, we define LS(v) to be the set of variables that appear in the left-hand side of production rules, where v appears in the left-hand side.

$$RS(v) = \begin{cases} \{x \mid v \to x \in P\} \cup \{(x, v_f) \mid v \to x \langle v_f \rangle \in P\}, & \text{if } v \in V_T, \\ \{v_t \mid v \to v_t \in P\} \cup \{(v_t, v_f) \mid v \to v_t v_f \in P\}, & \text{if } v \in V_F. \end{cases}$$

We say that two variables  $v_1$  and  $v_2$ , where  $v_1, v_2 \in V_T$  or  $v_1, v_2 \in V_F$  are right-indistinguishable if and only if  $RS(v_1) = RS(v_2)$ . It is easy to see that we do not change the language of G if we replace the occurrences of  $v_1$  and  $v_2$  with a new variable v' since two variables generate exactly the same structures.

$$LS(v) = \begin{cases} \{v_f \mid v_f \to v \in P\} \cup \{(v_{f_1}, v_{f_2}) \mid v_{f_1} \to vv_{f_2} \in P\}, & \text{if } v \in V_T, \\ \{(v_t, x) \mid v_t \to x \langle v \rangle \in P\}, & \text{if } v \in V_F. \end{cases}$$

We also define two variables  $v_1$  and  $v_2$  to be *left-indistinguishable* if and only if  $LS(v_1) = LS(v_2)$ . We say that two variables  $v_1$  and  $v_2$  are *indistinguishable* if they are right-indistinguishable or left-indistinguishable. Here we show that the language of the resulting NRHG does not change when we merge indistinguishable variables into a single variable.

**Theorem 1.** Given two indistinguishable variables  $v_1$  and  $v_2$  of an NRHG  $G = (\Sigma, V_T, V_F, P, s)$ , let G' be a new NRHG where all indistinguishable variables are merged according to indistinguishable classes of G. Then, L(G) = L(G').

We repeat the merging process until there is no pair of indistinguishable variables in the NRHG. Empirically, we have obtained about 80% size reduction by merging indistinguishable variables in primitive NRHGs. We show the experimental evidence in Sect. 5.

#### 3.3 Genetic Algorithm

We now have a primitive NRHG from a set of positive examples without any indistinguishable variables. Next, we need to make it as small as possible while considering a set of negative examples. Recall that our main goal is to compute a concise NRHG that generates all positive examples and does not generate all negative examples.

We employ a genetic algorithm (GA), which involves an evolutionary process, to find a small NRHG from a given primitive NRHG. In a genetic algorithm, we first make a population of candidate solutions called *individuals* and make it evolve to the population of better solutions by the help of genetic operators such as *structural crossover* and *structural mutation*.

We explain how these genetic operators work in our schema inference algorithm. We assume that every individual in the first population is indeed an NRHG with seven variables and thus encoded as a string of length 7.

- structural crossover: In the population, we randomly select two encoded individuals  $p_1$  and  $p_2$  as parents. We use  $p_1 = 1324133$  and  $p_2 = 2234144$  as a running example for explaining our approach.

$$p_1 = 1324133$$
 and  $p_2 = 2234144$ .

These strings encode two partitions  $\pi_{p_1}$  and  $\pi_{p_2}$  as follows:

 $\pi_{p_1}: \{1,5\}, \{3\}, \{2,6,7\}, \{4\} \text{ and } \pi_{p_2}: \{5\}, \{1,2\}, \{3\}, \{4,6,7\}.$ 

Namely, the *i*th number of  $p_1$  implies the index of the block where the *i*th variable of  $p_1$  belongs. For example, the third number of  $p_1$  is 2, and therefore, the variable 3 belongs to the second block #2 of  $\pi_{p_1}$ . Now we randomly select two blocks, say #2 and #4. The #2 block is copied from  $p_1$  to  $p_2$  by taking the union of #2 blocks in  $p_1$  and  $p_2$  and #2 block to be moved from  $p_1$ , and #4 block is copied from  $p_2$  to  $p_1$  in the same way. We obtain the following results:

 $\pi_{p'_1}: \{1,5\}, \{3\}, \{2\}, \{4,6,7\}, \pi_{p'_2}: \{5\}, \{1,2\}, \emptyset, \{3,4,6,7\}$ 

In this way, the number of blocks of each partition can diminish by merging randomly selected blocks.

- structural mutation: We randomly select an individual p = 1324133 and replace a character in the string by some random number. For example, if we replace the second character by 4, then the following offspring is produced:

$$\pi_{p'}: \{1,5\}, \{3\}, \{2,6,7\}, \{2,4\}.$$

We employ the GA approach for inferring a concise NRHG from a set of positive examples and a set of negative examples as follows:

- 1. Initialize the population of candidate solutions. Here we set the population size to, 1000. The initial candidate solutions are the primitive NRHGs reduced by merging indistinguishable variables.
- 2. Select some pairs of individuals according to the crossover rate (0.4) and construct new pairs of individuals by applying the crossover operator to the selected pairs.
- 3. Select some individuals according to the mutation rate (0.03) and modify the selected individuals by applying the mutation operator.
- 4. Calculate a fitness value f(p) for each individual p by the fitness function. Let p be an individual encoding for an NRHG  $G = (\Sigma, V_T, V_F, P, s)$ . Then, the fitness value f(p) of p is defined as follows:

$$f(p) = \begin{cases} \frac{1}{|V_F| + |V_T|} + \frac{1}{|P|} + \frac{|\{w \in U_+ \mid w \in L(G)\}|}{|U_+|}, & \text{if } U_- \cap L(G) = \emptyset, \\ 0 & \text{otherwise.} \end{cases}$$

where  $U_+$  is the set of positive examples and  $U_-$  is the set of negative examples.

- 5. Generate a next generation by *roulette-wheel selection* from the current population of solutions. Note that we retain the individuals from the best 10% of the current population unchanged in the next generation and select only the remaining 90% by roulette-wheel selection.
- 6. Iterate 1–5 steps until the fitness value of the best individual reaches the given threshold.

## 4 Converting NRHG into Relax NG Schema

Here we present a conversion algorithm from an NRHG into a corresponding Relax NG schema. A Relax NG schema uses references to *named pattern* using the **define** elements. Now tree or forest variables in NRHGs can be directly converted into the **define** elements for being used as references.

### 4.1 Horizontal NFA Construction

Given an NRHG  $G = (\Sigma, V_T, V_F, P, s)$ , let us consider the starting symbol s. Without loss of generality, we assume that there is a production rule  $s \to x \langle v_f \rangle \in P$ , where  $x \in \Sigma$  and  $v_f \in V_F$ . Then, we convert s into the corresponding define element in the resulting Relax NG schema. Now it remains to convert the forest variable  $v_f$  into the corresponding element in the schema.

We construct an NFA that accepts all possible sequences of tree variables that can be generated by  $v_f$ . We call this procedure the *horizontal NFA construction* for  $v_f$ . For each forest variable  $v_f \in V_F$ , where  $v_t \to x \langle v_f \rangle \in P$ , we construct a horizontal NFA  $A_{v_f} = (Q, \Sigma, \delta, q_0, q_f)$  as follows:

- 1.  $Q = V_F \cup \{q_f\}$  is a finite set of states,
- 2.  $\Sigma = V_T$  is an input alphabet,
- 3.  $q_0 = v_f$  is the initial state, and
- 4. the transition function  $\delta$  is defined as follows:
  - (a)  $q' \in \delta(q, v_t)$  for each  $q \to v_t q' \in P$ , and
  - (b)  $q_f \in \delta(q, v_t)$  for each  $q \to v_t \in P$ .

For example, Fig. 1 shows how we construct horizontal NFAs from a simple NRHG. From the first two production rules, we know that  $F_0$  generates a sequences of sub-elements of **records** and  $F_1$  generates a sequences of sub-elements of **car**. Therefore, we generate two horizontal NFAs  $A_{F_0}$  and  $A_{F_1}$  with the initial states are  $F_0$  and  $F_1$ , respectively.

### 4.2 State Elimination for Obtaining Regular Expressions

Recall that a Relax NG schema can specify a regular tree language when we consider the tree structures of XML documents captured by the schema. When a Relax NG schema describes a set of possible sequences of trees, we use several elements such as choice, group, zeroOrMore, and so on.



**Fig. 1.** Since two forest variables  $F_0$  and  $F_1$  are used for generating sequences of subelements of **records** and **car**, respectively, we construct two horizontal NFAs  $A_{F_0}$  and  $A_{F_1}$ . Note that the final states of  $A_{F_0}$  and  $A_{F_1}$  are merged into a single final state f.

The choice element implies that one of the sub-elements inside the element can be chosen. Therefore, we can say that the role of the choice element in Relax NG corresponds to the role of the union operator in regular expression. Similarly, the group element implies that the sub-elements inside the element should appear in exactly the same order. Thus, the group element corresponds to the catenation operator in regular expression. For this reason, we need to convert the obtained horizontal NFAs into the corresponding regular expressions since regular expressions are described in a very similar manner with the Relax NG schema.

State elimination is an intuitive algorithm that computes a regular expression from a finite-state automaton (FA) [9]. There are several heuristics of state elimination for obtaining shorter regular expressions from FAs [7–10]. Delgado et al. [7] observed that an order in eliminating states is crucial for obtaining a shorter regular expression. They defined the weight of a state to be the size of new transition labels that are created as a result of eliminating the state. We borrow their idea and define the weight of a state q in an FA  $A = (Q, \Sigma, \delta, s, F)$ as follows:

$$\sum_{i=1}^{\mathsf{IN}} \left( \mathbb{W}_{\mathsf{in}}(i) \times \mathsf{OUT} \right) + \sum_{i=1}^{\mathsf{OUT}} (\mathbb{W}_{\mathsf{out}}(i) \times \mathsf{IN}) + \mathbb{W}_{\mathsf{loop}} \times (\mathsf{IN} \times \mathsf{OUT})$$

where IN is the number of in-transitions excluding self-loops, OUT is the number of out-transitions excluding self-loops,  $W_{in}(i)$  is the size of the transition label on the *i*th in-transition,  $W_{out}(i)$  is the size of the transition label on the *i*th out-transition, and  $W_{loop}$  is the size of the self-loop label. After calculating the weights of all states, we eliminate the state with the smallest weight and calculate the state weights again. We repeat this procedure until there are only the initial state and the single final state.

#### 4.3 Schema Refinement

Now we have regular expressions for forest variables of an NRHG and are ready to convert these regular expressions into the form of Relax NG schema. We also use several additional techniques for converting an NRHG into a Relax NG schema.

- Replacing zeroOrMore elements by oneOrMore elements: The zeroOrMore element is used when there is optionally a repetition of a certain pattern like the Kleene star \* operator in regular expression. For example, a regular expression  $a^*$  can be converted using a zeroOrMore element and an element named a inside the zeroOrMore element. In some cases such as  $a^* \cdot a$  or  $a \cdot a^*$ , we can describe the pattern using the Kleene plus operator  $a^+$ . Since Relax NG schema supports the oneOrMore element that corresponds to the Kleene plus in regular expression, we can make the resulting schema smaller in some cases.
- Checking the dependency of forest variables: Consider two forest variables  $v_1$ and  $v_2$ , where  $v_2$  can be derived from  $v_1$ , but  $v_1$  cannot be derived from  $v_2$ . If we construct regular expressions for two forest variables, then there should be some redundancy in two regular expression since the pattern described for  $v_2$ is already contained in the pattern described for  $v_1$ . Therefore, we can write the pattern for  $v_2$  by just referring to the pattern for  $v_1$  instead of writing two redundant patterns.

## 5 Experimental Results

We conduct experiments for inferring a Relax NG schema from a given XML data. For the experiments, we use a Java library  $\times$ mlgen developed as a part of Sun Multi-Schema XML Validator<sup>1</sup> from randomly generating positive and negative XML instances for an input Relax NG schema.

### 5.1 Experimental Setup

We use three benchmark Relax NG schemas—XENC, XML-DSig, IBTWSH—to evaluate the performance of our Relax NG inference algorithm.

We aim at inferring only the relationship between elements from XML data. Therefore, we ignore the descriptions for attributes of XML data from benchmark schemas. Moreover, we manually replace the elements defined by the anyName name by the elements with the name anyName since otherwise randomly generated instances may have too many elements with arbitrary names. We also limit the maximum number of appearing sub-elements in the zeroOrMore elements to 2 since otherwise we may have very large XML instances compare to the size of input schema.

## 5.2 Size Reduction of NRHGs by Optimization

We show that the optimization process helps to reduce the size of primitive NRHGs generated by positive instances.

Table 1 exhibits that the optimization process reduce 84.15%, 82.13%, 77.04% of redundancy from the primitive NRHGs constructed from the positive instances of XENC, XML-DSig and IBTWSH, respectively. Note that the optimization process contributes to the speedup of the genetic process as the size of initial population also decreases substantially.

<sup>&</sup>lt;sup>1</sup> The Oracle Multi-Schema XML Validator (MSV). https://msv.java.net/.

Benchmark schema	XENC		XML-DSig		IBTWSH	
	Before	After	Before	After	Before	After
# of tree variables	755.17	123.67	1048.73	123.20	1222.86	162.57
# of forest variables	705.17	187.17	998.73	176.93	1122.86	208.29
# of production rules	1460.33	359.83	2047.47	349.13	2345.71	467.29
Average size of NRHG	4094.93	649.27	4691.43	838.14	2920.67	670.67
Compression ratio (%)	15.85		17.87		22.96	

**Table 1.** The compression ratio ([size of NRHG before optimization]/[size of NRHG before optimization]) achieved by merging indistinguishable variables from primitive NRHGs.

#### 5.3 Precision of Inferred Schema

For three benchmark schemas, we generate 50 positive instances and 25 negative instances by xmlgen. Note that we set the error rate to 1/100 when generating negative instances. Then we run our inference algorithm to infer Relax NG schemas for the instances. We repeat the process 100 times and calculate the average value.

We evaluate the precision of our inference system in two directions. First, we validate the inferred schema against 1,000 positive instances generated from the original benchmark schema. Second, we validate the inferred schema against 1,000 negative instances generated from the original benchmark schema. We expect that the inferred schema should generate the positive instances and not generate the negative instances if they are inferred closely to the original schemas.

Benchmark schema	XENC	XML-DSig	IBTWSH	IBTWSH
			(50/25)	(100/50)
Precision for positive instances (%)	91.98	93.50	46.05	96.87
Precision for negative instances (%)	82.43	83.85	83.45	74.67

 Table 2. The precision of our Relax NG schema inference system

Table 2 shows the precision of our inference algorithm. Note that the fourth column shows the results for the benchmark IBTWSH with 100 positive and 50 negative instances. Speaking of the first two results, precisions for positive and negative instances are very similar. The inferred schemas generate more than 90% of positive instances of the original schemas and do not generate more than 80% of negative instances. The performance is good considering that we infer schemas with only a small number of instances.

For the benchmark  $\mathsf{IBTWSH}$ , only 46.05 % of positive instances can be generated by the inferred schema. The inference precision improves significantly when we double the number of instances to 100 positive and 50 negative instances. We suspect that the reason why the precision for the benchmark IBTWSH is especially low is because IBTWSH schema has several interleave elements that allow the sub-elements to occur in any order. Since our inference system does not support the inference of interleave elements, it seems more difficult to infer schemas with interleave elements.

## 6 Conclusions

XML schemas are formal languages that describe structures and constraints about XML instances. They are crucial to maintain and manipulate XML documents efficiently—an XML document should conform a specific XML schema. However, in practice, we may not have a valid schema or have an incorrect schema. This has led many researchers to design an efficient schema inference algorithm.

We have presented an Relax NG schema—one of the most powerful XML schema languages—inference algorithm based on 1) a genetic algorithm for learning process and 2) state elimination heuristics for retrieving a concise Relax NG schema. We have implemented the proposed algorithm and measured the preciseness and conciseness of the algorithm using well-know benchmark schemas. Our experiments have showed that the proposed algorithm has 90% preciseness for accepting positive examples and 80% preciseness for rejecting negative examples. In future, we plan to consider other learning approaches for better performance and more Relax NG specifications such as interleave.

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